

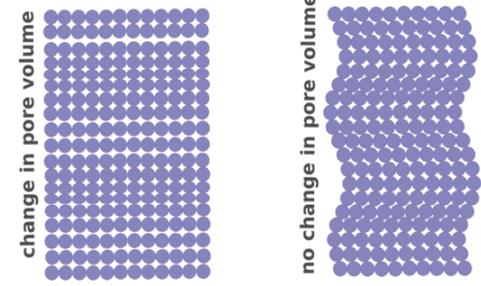
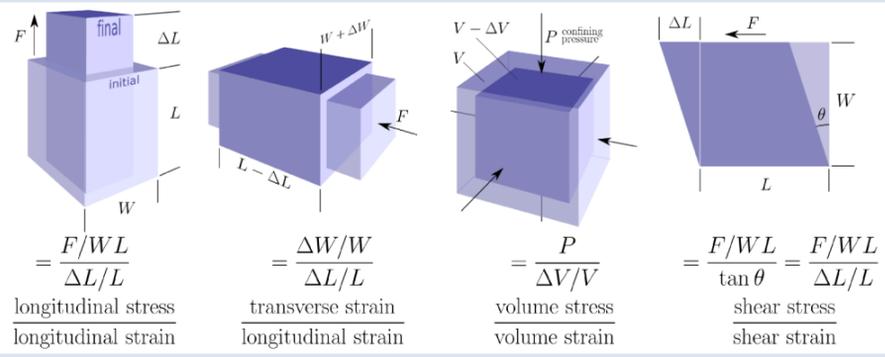
Elastic parameters	$E$ Young's modulus [kg·m <sup>-1</sup> s <sup>-2</sup> ]	$\nu$ Poisson's ratio [dimensionless] aka $\sigma$	$K$ bulk modulus [kg·m <sup>-1</sup> s <sup>-2</sup> ] aka volumetric modulus	$\mu$ shear modulus [kg·m <sup>-1</sup> s <sup>-2</sup> ] aka rigidity, $G$	$\lambda$ 1st Lamé parameter [kg·m <sup>-1</sup> s <sup>-2</sup> ] aka incompressibility	$V_P$ P-wave velocity [m/s] aka compressional vel	$V_S$ S-wave velocity [m/s] aka shear velocity	$\Gamma$ $V_P:V_S$ ratio [dimensionless]
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Engineers... ( $E, \nu$ )			$\frac{E}{3(1-2\nu)}$	$\frac{E}{2(1+\nu)}$	$\frac{E\nu}{(1+\nu)(1-2\nu)}$	$\sqrt{\frac{E(1-\nu)}{\rho(1+\nu)(1-2\nu)}}$	$\sqrt{\frac{E}{2\rho(1+\nu)}}$	$\sqrt{\frac{1-\nu}{\frac{1}{2}-\nu}}$
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Fluid substitution... ( $K, \mu$ )	$\frac{9K\mu}{3K+\mu}$	$\frac{3K-2\mu}{2(3K+\mu)}$			$K - \frac{2}{3}\mu$	$\sqrt{\frac{K + \frac{4}{3}\mu}{\rho}}$	$\sqrt{\frac{\mu}{\rho}}$	$\sqrt{\frac{K + \frac{4}{3}\mu}{\mu}}$
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Rock physicists... ( $\mu, \lambda$ )	$\frac{\mu(3\lambda+2\mu)}{\lambda+\mu}$	$\frac{\lambda}{2(\lambda+\mu)}$	$\lambda + \frac{2}{3}\mu$			$\sqrt{\frac{\lambda+2\mu}{\rho}}$	$\sqrt{\frac{\mu}{\rho}}$	$\sqrt{\frac{\lambda+2\mu}{\mu}}$
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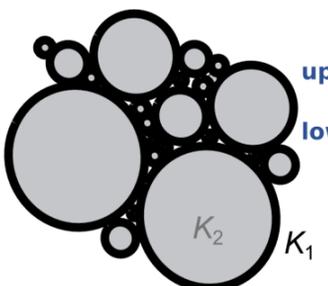
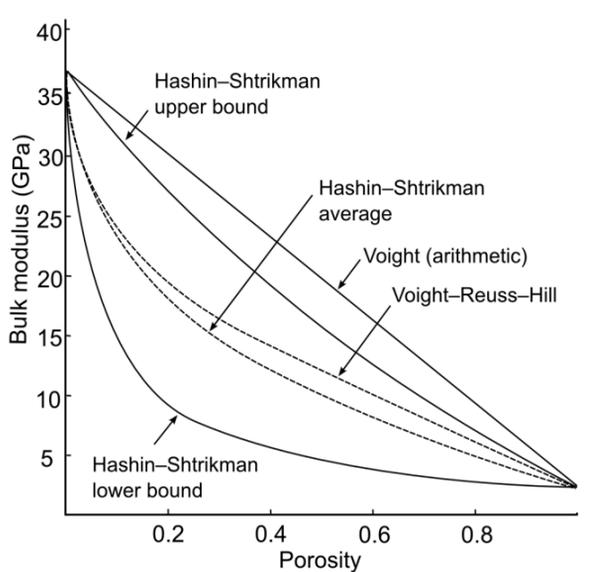
Geophysicists... ( $V_P, V_S$ )	$\rho V_S^2 \frac{(3V_P^2 - 4V_S^2)}{V_P^2 - V_S^2}$	$\frac{V_P^2 - 2V_S^2}{2(V_P^2 - V_S^2)}$	$\rho \left( V_P^2 - \frac{4}{3}V_S^2 \right)$	$\rho V_S^2$	$\rho (V_P^2 - 2V_S^2)$			$\frac{V_P}{V_S}$
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	Density [kg/m <sup>3</sup> ]	[GPa]	[dimensionless]	[GPa]	[GPa]	[GPa]	[m/s]	[m/s]	[dimensionless]
Quartz	2650	95	0.07	37	44	8	6008	4075	1.47
Feldspar (mean)	2620	40	0.32	37.5	15	28	4685	2393	1.96
Plagioclase	2630	70	0.35	76	26	59	6487	3144	2.06
Calcite	2710	84	0.32	77	32	56	6645	3436	1.93
Dolomite	2870	117	0.30	95	45	65	7349	3960	1.86
Anhydrite	2980	72	0.23	45	29	26	5299	3120	1.70
Siderite	3960	135	0.32	124	51	90	6963	3589	1.94
Pyrite	4930	305	0.15	147	132	59	8094	5174	1.56
Sandstone, 10 p.u.	2500	32-105	~0.05-0.10	15-18	7-24	1-3	2500-4500	1725-3103	~1.45-1.5
Limestone, 10 p.u.	2540	97-280	~0.33	37-71	9-26	18-53	3800-6500	1900-3250	~2.0
Shale, 5 p.u.	2500	20-160	~0.27	16-36	2-19	3-24	1800-5000	1000-2777	~1.8
Water (brine)	1030	0	0.5	2.3	0	2.3	1507	0	undefined
Oil (40 API)	830	0	0.5	1.6	0	1.6	1226	0	undefined

### Hashin-Shtrikman

Upper and lower bounds



**upper bound when**  
 $K_1 > K_2$   
**lower bound when**  
 $K_1 < K_2$

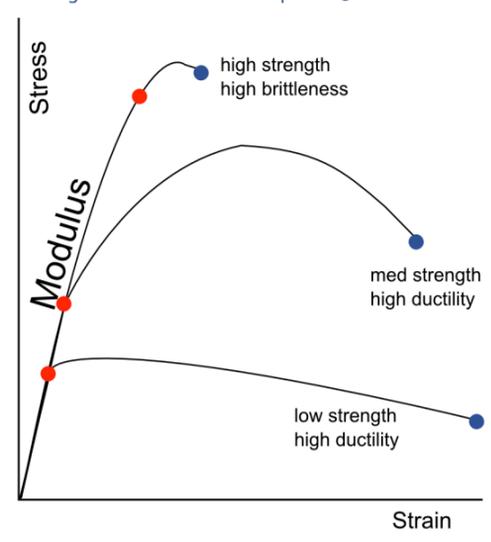
$$K^{HS\pm} = K_1 + \frac{f_2}{(K_2 - K_1)^{-1} + f_1(K_1 + \frac{4}{3}\mu_1)^{-1}}$$

$$\mu^{HS\pm} = \mu_1 + \frac{f_2}{(\mu_2 - \mu_1)^{-1} + \frac{2f_1(K_1 + 2\mu_1)}{5\mu_1(K_1 + \frac{4}{3}\mu_1)}}$$

Get upper bound and lower bounds by switching indices  
upper:  $K_1 = K_1, K_2 = K_2$  lower:  $K_1 = K_2, K_2 = K_1$   
 $f_1$  and  $f_2$  is volume fraction of constituent 1 and 2.

### Strength and brittleness

Modulus is the slope below the elastic limit ●  
Strength is stress at failure point ●



**Bulk density**  $\rho = (1 - \phi)\rho_S + \phi\rho_F$   
 $\rho_S$  density of the solid,  $\rho_F$  density of the fluid,  
 $\phi$  is porosity

**Fluid modulus**  $\frac{1}{K_f(P, T)} = \sum_i \frac{S_i}{K_i(P, T)}$   
for a mixture of fluids with fractions  $S_i$ , fluid bulk moduli depend on temperature  $T$  & pressure  $P$

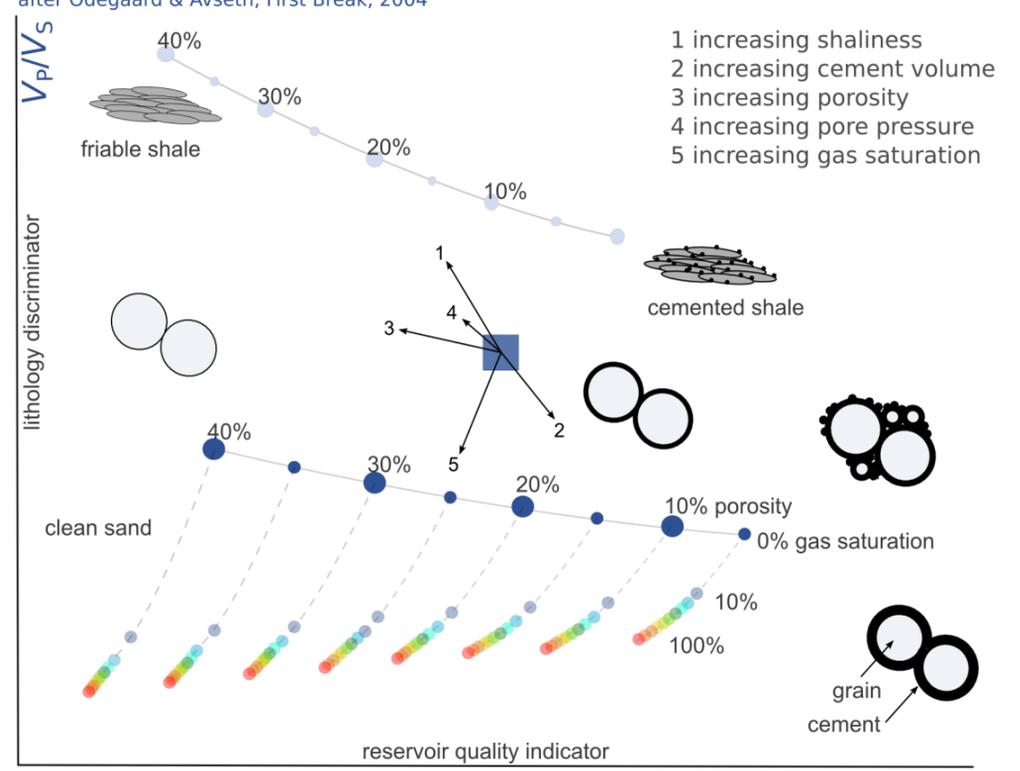
**Gassmann's equation**  
Fluid substitution

$$K_{eff} = K_{dry} + \frac{\left(1 - \frac{K_{dry}}{K_{min}}\right)^2}{\frac{1 - \frac{K_{dry}}{K_{min}} - \phi}{K_{min}} + \frac{\phi}{K_f}}$$

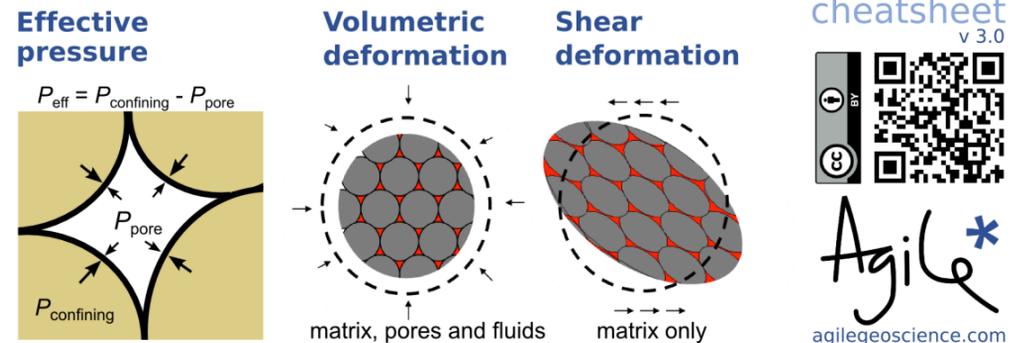
$$K_{dry} = \frac{1 + \left(K_{eff} \frac{\phi - 1}{K_{min}} - \frac{\phi}{K_f}\right)}{\frac{1 - \frac{K_{eff}}{K_{min}} + \phi}{K_{min}} - \frac{\phi}{K_f}}$$

### $V_P/V_S$ P-impedance template

Conceptual trends for siliciclastic lithologies at constant confining pressures  
after Odegaard & Avseth, First Break, 2004



P-impedance:  $\rho V_P$



ROCK PHYSICS  
cheatsheet  
v 3.0

Agile\*

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